# Single Period Integer Relaxation Examples 

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## Separate Dispatch and Pricing Runs

- Make no modifications to resource

Dispatch Run parameters

- Determine desired dispatch points
- Do not calculate prices


## Pricing Run

- Modify resource parameters
- Calculate prices


## Example \#1

- Load equals 455 MW
- Fixed costs (start-up and no-load) are considered in setting the price.
- Assume all resources are eligible for integer relaxation treatment
- Note: Offline resources do not participate in pricing

Example \#1: Offer Blocks (MW) \& Fixed Costs Any resource that is "committed" must run at least at its minimum


The Commitment and Dispatch Run: Example \#1


## Pricing Run Offer Modifications for Example \#1

- Allow resources to be partially committed for pricing calculations:
- Equivalently, resources are allowed to be fully dispatchable between 0 and their economic maximums.
- Start-up and No-load costs of $X$ and $Y$ are considered in setting the price.
- Equivalently, the bid blocks of Resources $X$ and $Y$ can be modified to incorporate the proportional start-up and no-load costs.
- For example, under integer relaxation with a single offer block, in the pricing run the total offer cost of dispatching a resource is:

$$
\begin{aligned}
\text { Total Offer Cost }= & \text { Incremental Energy Cost } \times \text { Dispatch }+ \\
& \text { Startup Cost } \times \text { Commitment Status }+ \\
& \text { Noload Cost } \times \text { Commitment Status }
\end{aligned}
$$

Where:

$$
\text { Commitment Status }=\frac{\text { Dispatch }}{\text { Economic Maximum }}
$$

## Pricing Run Offer Modifications for Example \#1

- As a result, the total offer cost of dispatching a resource in the pricing run can be rewritten as:

Total Offer Costs $=$ Incremental Energy Cost $\times$ Dispatch +

$\frac{\text { Noload Cost }}{\text { Economic Maximum }} \times$ Dispatch

- A resource's equivalent offer is equal to the sum of all three components in the boxes above.

Pricing Run Equivalent Offers for Example \#1


## Pricing Run Integer Relaxation LMP: Example \#1

```
Load = 455 MW
```

\$/MWh

| Load $=455$ MW |
| :--- |
| - The price is set by the modified |
| block 1 of Y. |
| - Integer Relaxation LMP = |
| \$233/MWh |

- The integer relaxation LMP is set by the first block of Resource Y, which includes its start-up and no-load costs in the price
- The dispatch MWs for all resources come from the dispatch run where Resource $X$ and $Y$ incur their full start-up and no-load costs
- Resource $Y$ will need a make-whole payments since it is only recovering part of its start-up and no-load costs through the price since it is not being dispatched at its economic maximum

The Integer Relaxation LMP is calculated at $\$ 233 / \mathrm{MWh}$.

| Asset | Commit. | Dispatch <br> $\mathbf{( M W )}$ | EcoMax <br> $\mathbf{( M W )}$ | Total Offer <br> Cost (\$) | Payment <br> $\mathbf{( \$ )}$ | MWP <br> $\mathbf{( \$ )}$ | LOC <br> $\mathbf{( \$ )}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{W}$ | On | 260 | 260 | 13,270 | 60,580 | 0 | 0 |
| $\mathbf{X}$ | On | 145 | 180 | 38,845 | 33,785 | 5,060 | 820 |
| $\mathbf{Y}$ | On | 50 | 150 | 15,000 | 11,650 | 3,350 | 0 |

Both $X$ and $Y$ receive a make-whole payment to make them whole to their total offer cost.
In addition, $X$ receives a LOC payment since at X's offer prices of $\$ 60-\$ 65 / M W h$, it would want to produce at its economic maximum at a $\$ 233 / M W h$ clearing pricing since it would make a profit of $\$ 820$.

## Example \#2

- Load equals 455 MW
- Fixed costs (start-up and no-load) are considered in setting the price.
- Assume all resources are eligible for integer relaxation treatment
- Note: Offline resources do not participate in pricing

Example \#2: Offer Blocks (MW) \& Fixed Costs
Any resource that is "committed" must run at least at its minimum


The Commitment and Dispatch Run: Example \#2


## Pricing Run Offer Modifications for Example \#2

- Allow resources to be partially committed for pricing calculations:
- Equivalently, resources are allowed to be fully dispatchable between 0 and their economic maximums.
- Start-up and No-load costs of $X$ and $Y$ are considered in setting the price.
- Equivalently, the bid blocks of Resources $X$ and $Y$ can be modified to incorporate the proportional start-up and no-load costs.


## Pricing Run Equivalent Offers for Example \#2



## Pricing Run Integer Relaxation LMP: Example \#2



- The integer relaxation LMP is set by the first block of Resource Y , which includes its start-up and no-load costs in the price
- The dispatch MWs for all resources come from the dispatch run where Resource X and Y incur their full start-up and no-load costs
- Resource $Y$ will not need a make-whole payment since it is being dispatched to its economic maximum in the dispatch run and is recovering its entire start-up and no-load costs through the price


## The Integer Relaxation LMP is calculated at $\$ 250 / \mathrm{MWh}$.

| Asse <br> $\mathbf{t}$ | Commit. | Dispatch <br> (MW) | EcoMax <br> (MW) | Total Offer <br> Cost (\$) | Payment <br> $\mathbf{( \$ )}$ | MWP <br> $\mathbf{( \$ )}$ | LOC <br> $\mathbf{( \$ )}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\mathbf{W}$ | On | 255 | 260 | 12,990 | 63,750 | 0 | 970 |
| $\mathbf{X}$ | On | 100 | 180 | 36,000 | 25,000 | 11,00 <br> 0 | 3,880 |
| $\mathbf{Y}$ | On | 100 | 100 | 25,000 | 25,000 | 0 | 0 |

Resource X receives a make-whole payment to make it whole to its total offer cost.
In addition, Resource W and X receive a LOC payment since at Resource W's and X's offer prices of \$50-\$56/MWh and $\$ 60-\$ 65 / \mathrm{MWh}$, they would want to produce at their economic maximums at a $\$ 250 / \mathrm{MWh}$ clearing pricing since they would make a profit of $\$ 970$ and $\$ 3,880$, respectively.

